Theoretical Studies of Boranamine and Its Conjugate Base. Comparison of the B-N and B-P π **Bond Energies**

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To answer questions that have arisen about the relative strengths of the B-N and B-P π bonds, we have investigated $BH₂NH₂$ and $BH₂NH⁻$ by the methods of ab initio molecular electronic structure theory, using basis sets of high quality, and we have characterized them with respect to their molecular geometries, energies, dipole moments, normal vibrational modes, and harmonic vibrational frequencies. With the aid of the latter we have been able to resolve several disagreements in the literature on the interpretation of the $BH₂NH₂$ infrared absorption spectrum. Aminoborane has two rotational transition states, one of **C,** symmetry at **32.4** kcal/mol above the planar ground state and one of *C2"* symmetry at **37.9** kcal/mol. The former has a BNH angle of **l10So** and an out-of-plane angle at nitrogen of **55.4'.** Surprisingly, it is the d orbitals of the nitrogen atom that give the *C,* transition state its lower energy and its approximately tetrahedral geometry at nitrogen. The BH₂NH⁻ anion has planar geometry and a BN bond length of **1.366 A.** It has an inversion transition state at **20.8** kcal/mol above the ground state, but it has no rotational transition state. Finally, comparison of BH_2NH_2 and BH_2PH_2 shows that the B-P π bond is stronger than the B-N π bond (40.5 versus 37.9 kcal/mol). Furthermore, it is shown that these bonds are overwhelmingly of $p\pi$ -p π type.

Introduction

In our studies^{1,2} of borylphosphine, $BH₂PH₂$, we made a series of comparisons with its nitrogen analogue, boroanamine, $BH₂$ -NH₂. Quite a bit is known about the latter molecule; for example, the structure³ and vibrational frequencies^{$4-8$} of the ground state have been determined experimentally. But for some properties, especially those relating to transition states and to the strength of the boron-nitrogen π bond, one must rely on theoretical investigations with small basis sets that gave inconsistent results. Even less is known about the anion $BH₂NH⁻$. To rectify this situation we have undertaken a thorough study of $BH₂NH₂$ and $BH₂NH₋$. The results shed new light on the surprisingly strong boron-phosphorus π bond. They are also useful in the assignment of experimental vibrational frequencies to the various normal modes of $BH₂NH₂$.

Method

The Gaussian series of programs⁹ was used throughout. Methods and options were selected by standard keyword choices. The Z-matrix approach was used to specify molecular geometry.

The following three basis sets were employed: (a) The DZ **set** used the contracted double- ζ Gaussian basis set of Huzinaga, Dunning, and

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Mellon University: Pittsburgh, PA, 1983. Frisch, M. J.; Binkley, J. S.;
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Hay¹⁰⁻¹² with the hydrogen atoms scaled by a factor of 1.2. (b) The DZ + P basis set was formed from the preceding set by adding **six** d functions $(a = 0.7)$ for boron, six d functions $(\alpha = 0.8)$ for nitrogen, and three p functions $(\alpha = 0.75)$ for each hydrogen atom. It may be described as B(9s5pld/4s2pld), N(9s5pld/4s2pld), H(4slp/2slp). (c) The DZ + $2P + diff$ basis set, with two sets of polarization functions as well as diffuse functions on the heavy atoms, was formed from the DZ basis set by adding one s function $(\alpha = 0.019)$, one set of p functions $(\alpha = 0.019)$, and two sets of d functions $(\alpha = 0.45 \text{ and } 0.95)$ for boron; by adding one **s** function $(\alpha = 0.048)$, one set of p functions $(\alpha = 0.048)$, and two sets of d functions (α = 0.55 and 1.05) for nitrogen; and by using the DZ + P basis set for hydrogen.

The restricted self-consistent-field (SCF) method with an analytic gradient method was used **to** determine the moiecular geometry. Analytic second derivatives of the SCF wave function were used **to** determine the harmonic vibrational frequencies and corresponding normal modes. Configuration interaction wave functions (CISD) including all singly and doubly excited configurations (except that inner-shell molecular orbitals were frozen) were obtained at the optimized **SCF** geometries. The Davidson correction¹³ was used to estimate the effect on the molecular energy of unlinked quadruple excitations. (In the following text all energies are Davidson-corrected energies.) After a preliminary geometry with the DZ basis set was obtained, the structure was refined with the DZ + P basis set and, for the $BH₂NH₂$ ground state and the $BH₂NH₋$ anion, the $DZ + 2P + diff$ basis set.

To obtain more accurate vibrational frequencies for the ground state of BH₂NH₂, a second-order Møller-Plesset (MP2) correlation energy correction was used, with no frozen orbitals.

Ground State of the BHzNHz Molecule

Aminoborane has an ethylene-like planar ground state, **1.** Our results for the properties of this state are listed in Table I. For comparison, the *r,* structural parameters determined experimentally3 are as follows: r(BN), **1.391(2) A;** r(BH), **1.195(4) A;** $r(NH)$, 1.004(2) A; $\theta(HBH)$, 122.2(2)^o; $\theta(HNH)$, 114.2(2)^o. We regard the agreement between experiment and theory as satisfactory.

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Table I. Properties of the BH_2NH_2 ¹A₁ Ground State⁴

		MP ₂	
	$DZ + P$	$DZ + 2P + diff$	$DZ + P$
$r_c(BN)$	1.395	1.393	1.399
$r_{e}(\text{BH})$	1.194	1.194	1.191
$r_c(NH)$	0.996	0.995	1.011
$\theta_e(NBH)$	119.4	119.2	118.6
$\theta_e(HBH)$	121.2	121.5	122.7
$\theta_e(BNH)$	123.1	123.0	123.2
θ_e (HNH)	113.9	114.0	113.6
dipole moment	1.74	1.68	1.72

Bond lengths are in **A,** angles are in deg, and dipole moments are in D.

In Table I1 we list the vibrational frequencies of aminoborane, both theoretical and experimental. Assignments of the two experimental B_1 frequencies require explanation. In their original paper⁴ Gerry and co-workers state that "... the intense central spike of the C-type fundamental ν_7 at 1005 cm⁻¹ (the BH₂ outof-plane wagging motion) is obvious." However, in their Table I the 1005-cm⁻¹ frequency was assigned to the $NH₂$ wag, and this assignment was carried forward in later work.⁵ In ref 6, which represents the current view of the University of British Columbia group,⁷ the B_1 assignments are reversed, and the 1005-cm⁻¹ frequency is assigned to the BH₂ wag. Our theoretical results are in agreement with these latest assignments. (Assignment of the gas-phase 1005 -cm⁻¹ frequency to the BH₂ out-of-plane wag has been previously suggested by Carpenter and Ault,⁸ who have also noticed the difference in ref 4 between text and table.)

With this reassignment there is satisfactory agreement between theory and experiment, the mean deviations being 7.5%, 7.2%, and 4.6% for the comparisons of columns 4,5, and 6, respectively, with column 7. Previous workers^{14,15} have found that for smaller molecules one can expect differences of \sim 4% between MP2 (DZP) harmonic frequencies and "experimental" harmonic frequencies if available. Also, in each case the result for the theoretical harmonic frequency lies above the experimental frequency, as is typical in studies of this kind.

In a study of the $BH₂NH₂$ planar ground state using a 3-21G basis set, Ha¹⁶ reports that the higher B_1 frequency (1102 cm⁻¹) is the NH_2 wag and the lower one (828 cm⁻¹) is the BH_2 wag, a conclusion opposite to that reached above. We have repeated this work, and although weobtain thesameSCFenergyas reported by Ha, we again find that the higher B_1 frequency is the BH_2 wag (albeit mixed with a relatively small contribution from the $NH₂$ wag) and the lower frequency is the $NH₂$ wag, consistent with our results using larger basis sets. Furthermore, the 3-21G frequencies we obtain are somewhat different from those reported by Ha. The two B_1 frequencies are 1103 and 821 cm⁻¹. The others are as follows (cm^{-1}) : A₁, 3736, 2700, 1831, 1438, and 1227; A₂, 874; B₂, 3827, 2768, 1241, 805.

Our results shed some light **on** two other reassignments of the gas-phase experimental frequencies⁴ proposed by Carpenter and Ault:*

(1) They suggest reassignment of the 1131-cm⁻¹ band^{4,5} (most recent gas-phase observation⁶ at 1122.2 cm⁻¹) from ν_{11} to ν_5 , the BH₂ symmetric bend. Our MP2 (DZ + P) result for ν_{11} (1161) cm^{-1}) is closer to either 1131 or 1122.2 cm⁻¹ than is our result

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Table II. Vibrational Frequencies and Intensities of the BH₂NH₂ ¹A₁ Ground State^a

		SCF			
sym	normal mode ^b	$DZ + P$	DZ + $2P +$ diff	MP ₂ $DZ + P$	$ext{ext}$ (gas phase)
ν_1 A ₁	NH sym str	3840	3822	3674 (39)	3451
ν_2	BH sym str	2676	2659	2667 (94)	2495
ν_3	$NH2$ sym bend + BN str	1765	1770	1660 (80)	1617
ν_4	BN str + $BH2$ sym bend - $NH2$ sym bend	1416	1420	1374 (58)	1337.47
v.	$BH2$ sym bend $-$ BN str	1214	1211	1181 (< 1)	1145
ν_6 A ₂	torsion	867	864	887 (0)	837 ^o
$\nu_7 B_1$	$BH2$ wag	1114	1110	1062 (21)	1004.68
ve	$NH2$ wag	625	624	619 (211)	612.20s
ν_9 B_2	NH asym str	3946	3927	3789 (37)	3533.8
v_{10}	BH asym str	2748	2730	2765 (153)	2564
v_{11}	$NH2$ rock – BH ₂ rock	1216	1216	$1161d$ (36)	1122.2
v_{12}	$BH2 rock + NH2 rock$	792	789	$754d$ (<1)	742 vw

^a Harmonic vibrational frequencies are in cm⁻¹ for ¹¹B, ¹⁴N, and ¹H isotopes. The molecular plane is taken as theyz plane. Infrared intensities in km mol⁻¹ are shown in parentheses. ^b Where motion of more than one internal coordinate makes a significant contribution to the normal mode, they are listed in order of decreasing importance. Plus and minus signs indicate relative phases. The rocking (asymmetric bending) motions are considered in phase if two H atoms move toward each other. The NH2 symmetric bend and BN stretch are considered in phase if the N atom moves toward the H atoms as the HNH angle increases. c Frequencies from ref 6; intensities from ref 5.^d The two motions have about equal weight. e Reference 5: "Value estimated from appearance of perturbation." *I* The two B₁ assignments in ref 4 and 5 have been reversed-see text.

for ν_5 (1181 cm⁻¹), and therefore we tend to side with the original assignment. (Thedifferences are rather small, and the agreement is excellent in either case.) Furthermore, in support of their proposed reassignment Carpenter and Ault cite the observation by Gerry and co-workers⁴ of "overlapping and additional structure belonging to the ¹⁰B species." We can explain this observation **on** the basis of our results. We find that there is a strong component of BH₂ rock in ν_{11} ; in fact, with the MP2 (DZ + P) method, the $NH₂$ rock and $BH₂$ rock contribute about equally to ν_{11} and ν_{12} .

(2) They suggest reassignment of the gas-phase 1225-cm-l band^{4,5} (most recent gas-phase observation⁶ at 1145 cm^{-1}) from v_5 , the BH₂ symmetric bend, to an overtone of one of the fundamental frequencies, on the basis of a ¹⁵N shift observed for an argon matrix band at 1216 cm^{-1} . However, we find that the BN stretch contributes significantly to ν_5 and that might explain the ¹⁵N shift. Our MP2 (DZ + P) result of 1181 cm⁻¹ for ν_5 is consistent with the newer experimental result⁶ of 1145 cm^{-1} , and we are therefore inclined to support that assignment. A definitive resolution of the ν_5 assignment will probably be difficult because our predicted intensity indicates that it is very weak and it could be masked by an overtone or combination band.

A proposal by Brint and co-workers¹⁷ to interchange the assignments of ν_8 and ν_{12} was based on the earlier experimental data⁴ which had $\nu_8 > \nu_{12}$. The newer data^{5,6} have $\nu_8 < \nu_{12}$ in agreement with the theoretical results, and thus no interchange is necessary.

The vibrational intensities in Table I1 may be of use in sorting out any remaining ambiguities in assigning the various vibrational bands. At this point we have only the designations "strong" for ν_8 and "very weak" for ν_{12} in ref 5, and these are consistent with the theoretical intensities. (In addition, ν_6 is of course infraredinactive.)

Transition States of BH₂NH₂

The $BH₂NH₂$ molecule has two rotational transition states, one of lower energy and *Cs* symmetry, *2,* and one of higher energy

⁽¹⁷⁾ Brint, **P.;** Sangchakr, B.; Fowler, P. W. J. Chem. *Soc.,* Faraday Trans. *2 1989, 85,* **29.**

and C_{2v} symmetry, 3. The former has an out-of-plane angle at nitrogen of 55.4° and a BNH angle of 110.5°, and it lies 32.4 kcal/mol above the planar ground state. The latter is at **37.9** kcal/mol, and thus relaxation of the nitrogen atom from trigonal planar to approximately tetrahedral geometry lowers the energy by *5.5* kcal/mol. Surprisingly, almost all of this energy difference must be ascribed to the effect of polarization functions, for with a **DZ** basis set the corresponding energy change is only **0.2** kcal/ mol (from **39.7** to **39.5** kcal/mol) and there is very little change in geometry. (The BNH angle decreases slightly in going from **3** to **2**, (122.8° to 121.8°), and the out-of-plane angle at nitrogen of **2** is only **15.8O.)** The properties of these two transition states are summarized in Table 111. It should be noted that **3** is also a transition state for inversion of **2** to its equivalent form. Previous results for the two rotational energy barriers are as follows (kcal/mol): C_s , 33.3,¹⁸ 29.4,¹⁹ 33.0;²⁰ C_{2v} , 40.5,¹⁸ 43.1,¹⁹ 38.3,²⁰, **33AZ1**

There is a striking contrast between the **C,** rotational transition states of $BH₂NH₂$ and its phosphorus analogue, $BH₂PH₂$. With the **DZ** + P basis set, the latter is only **10.0** kcal/mol above the nonplanar ground state and only **4.1** kcal/mol above the planar form.² Its BPH angles are 94.8°, and its out-of-plane angle at phosphorus has the extremely high value of 82.9^o, in keeping with the well-known tendency of tervalent phosphorus to approach an orthogonal geometry. On the other hand the C_{2v} transition states of $BH₂NH₂$ and $BH₂PH₂$ are remarkably similar, with energies of **37.9** and **40.5** kcal/mol,2 respectively, above the planar forms. As measures of π -bond energies, these C_{2v} barriers are of particular importance; we shall return to this point in a later section.

Addition of polarization functions has relatively little effect on the BH2PH2 rotational barriers. With a **DZ** basis set, they are 9.6 (C_s) and 40.8 (C_{2v}) kcal/mol above the planar form,²² compared to the **4.1** and **40.5** kcal/mol noted above with the **DZ** $+$ P basis set. For the C_s rotational transition state, the outof-plane angles at phosphorus are **80.2O (DZ)** and **82.9" (DZ** + P). It thus appears that d orbitals on the nitrogen atom, but not **on** the phosphorus atom, are important for nonplanarity.

To better understand the role being played by the polarization functions in establishing the pyramidal geometry about N and P, we first examined the molecular orbitals. In $BH₂NH₂$ the coefficients of the nitrogen d orbitals in the occupied molecular orbitals are really quite small. In this respect a little bit goes a long way. (The coefficient of largest magnitude was **-0.0346** for d_{xz} in the la" MO.) We surmise that the main effect of the d orbitals **on** N is to concentrate the lone pair and bonding orbitals in **space,** thus reducing interpair repulsions and allowing the outof-plane angle at nitrogen to increase.

Figures 1 and **2** present contour diagrams of the difference in electronic density between calculations with and without polarization functions for $BH₂NH₂$ and $BH₂PH₂$, respectively. The molecular geometry in each case was that optimized for the *C,* transition state structure with the **DZ** + P basis set. The contours are displayed for a slice through the molecule containing the $BH₂$ plane. The $BH₂$ plane bisects the $NH₂$ ($PH₂$) angle for the C_s structure, and the prominent feature in solid contours **on** the

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- **(22)** Allen, T. L.; Fink, W. H. Unpublished work.

Table **III.** Properties of BH

I ₂ NH ₂ Rotational Transition States [®]			
C. transition state. ¹ A'	C_{2n} transition state, ${}^{1}A_1$		
1.471	1.458		
BH ₁ , 1.196	1.203		
1.221			

 α All results were obtained with the DZ + P basis set. See footnotes of Tables I and II for units, etc. For C_{2v} symmetry, the BH₂ group is in the *yz* plane. ^b The out-of-plane angle at N is the angle between the BN axis and the NH_2 plane. ϵ Energies are in kcal/mol relative to the planar ground state. $\frac{d}{dt}BH_2$ rock - NH_2 wag. \cdot NH₂ wag + BH₂ rock.

Figure 1. Difference electronic density for the $BH₂NH₂ C_r$ rotational transition state, in a plane passing through the $BH₂$ nuclei. Contours are shown for the difference in electronic density between calculations with and without polarization functions $(DZ + P - DZ)$. BH₂ (left) and N (right) nuclei in the plane are indicated by +. Projections onto the plane of NH2 hydrogen nuclei are indicated by *0.* Contour maximum is 0.05 e/\mathbf{A}^3 , and contours decrease at 0.01 e/\mathbf{A}^3 intervals. Solid curves indicate an increase in electronic density on adding polarization functions; dashed curves indicate a decrease.

right may be identified with the respective lone pairs. We also examined contours in the plane perpendicular to this **one,** and in the $NH₂$ plane, but in the interest of economy present only these which provide the greatest insight. The positive **contours**

⁽¹⁹⁾ Dill, **J.** D.; Schleyer, P. **v. R.;** Pople, J. A. *J. Am. Chem. Soc.* **1975,97, 3402.**

Figure 2. Difference electronic density for the $BH₂PH₂ C_s$ rotational transition state, in a plane passing through the $BH₂$ nuclei. The same conventions were followed as in Figure **1,** except that P replaces N.

correspond with those regions of space which have augmented electron density upon addition of the polarization functions to the basis set, and the dashed contours correspond with those regions of space which have had electron density removed to accomplish these augmentations. A small square is plotted at the location of the projection of the hydrogens attached to nitrogen (phosphorus) into this plane. It is clear that the effect of the addition of the polarization functions to the basis set has **been** to move some electron density from the region between the amino (phosphino) hydrogens and the BN (P) bond into the lone pair. In both figures the maximum positive contour plotted is 0.05 electron/ \hat{A}^3 . This value is approximately the maximum change observed in the region of the phosphorus lone pair, but the nitrogen changecontinues to increase to about **0.2** electron/A3 in contours not shown to enhance legibility. These contour diagrams confirm the greater importance of d orbitals **on** nitrogen over their role on phosphorus for this basis set.

The BH₂NH⁻ Anion

The conjugate base of aminoborane, $BH₂NH₋$, has a planar ground stateof *C,* symmetry, **4.** It also has an inversion transition

state of C_{2v} symmetry, 5. In these respects it resembles its phosphorus analogue, BH₂PH^{-1,2} But unlike BH₂PH⁻ it has no rotational transition state. The properties of **4** and **5** are summarized in Table IV. It may be **seen** that, with the largest basis set, the inversion transition state lies **20.8** kcal/mol above the ground state. This is much lower than the corresponding figure for BHzPH-, **53.5** kcal/moL2

We studied a constrained rotational transition state, **6,** in which the BNH angle was fixed at the same value as in the planar

$$
\mathbf{H}_{\mathbf{H}} = \mathbf{B} - \mathbf{M} \mathbf{H}
$$

Table **IV.** Properties of the BH2NH- Ground and Inversion Transition States'

	ground state, ¹ A'	inversion, ${}^{1}A_1$
$r_{\rm e}({\rm BN})$	1.366 (1.366)	1.329 (1.328)
$r_{\rm e}$ (BH)	BH ₁ , 1.244 (1.246)	1.259 (1.258)
	BH ₂ , 1.235 (1.234)	
$r_{\rm e}(NH)$	1.010 (1.009)	0.978 (0.978)
$\theta_e(NBH)$	NBH ₁ , 125.5 (124.6)	125.1 (124.8)
	NBH ₂ , 121.6 (121.7)	
θ_e (HBH)	112.9 (113.7)	109.9 (110.4)
$\theta_e(BNH)$	110.7 (110.9)	180.0 (180.0)
prot aff/energy, SCF ^b	17.52 (17.29)	21.5(19.8)
prot aff/energy, CISD ^b	17.41 (17.11)	22.9 (20.5)
prot aff/energy, Davidson cor ^b	17.33 (17.02)	23.4 (20.8)
dipole moment ^e	1.57(1.72)	1.79(1.30)
vibrational freq, v_e		
NH str	3661 (3655), A'	4169 (4131), A ₁
sym BH str	2392 (2377), A'	2256 (2239), A ₁
asym BH str	2301 (2265), A'	2127 (2091), B ₂
$BN str + sym BH2$ bend	1510 (1491), A' d	1582 (1551), A ₁
sym $BH2$ bend – BN str	$1253(1238)$, A' ^e	1302 (1287), A_1
BNH bend – $BH2$ rock	1201 (1179), A'	1049i (995i), B ₂
$BH2$ wag	1048 (1046), A"	1060 (1061), B ₁
torsion	977 (950), A"	489 (514) , B ₁
$BH2 rock + BNH$ bend	884 (874), A'	1032 (1011), B ₂ ^h

a Results with the $DZ + 2P +$ diff basis set are listed in parentheses; other results were obtained with the $DZ + P$ basis set. See footnotes of Tables I and II for units, etc. δ The proton affinity of the ground state is the energy in eV relative to the planar BH₂NH₂ ground state with the same basis set. The energy of the inversion transition state is in kcal/mol relative to the $BH₂NH-$ ground state. c The dipole moment is taken with respect to the center of mass. $\frac{d}{dx}BN \, \text{str} + \text{sym } BH_2 \text{ bend} + \text{BNH } bend.$ s sym BH₂ bend - BN str - BNH bend. f BNH in-plane bend. s BNH out-of-plane bend. h BH₂ rock + BNH in-plane bend.

ground state and the other geometrical parameters wereoptimized. With the largest basis set it was **30.3** kcal/mol above the ground state, or *9.5* kcal/mol above the inversion transition state. But when theconstraint was removed, the anion relaxed to theinversion transition state. In fact, the BNH force decreased monotonically as the BNH angle was changed from **85** to **180'.**

For the related molecules HN=NH and HP=PH it has been noted previously that the inversion barrier lies below the rotation barrier for the nitrogen compound, while the opposite is true of the phosphorus compound.23 A similar situation holds for $BH₂NH⁻$ and $BH₂PH⁻$, except that with $BH₂NH⁻$ one can obtain the rotational transition state only by means of a constraint. *As* a consequence, the $BH₂NH⁻$ inversion transition state has only one imaginary vibrational frequency, compared to two for the corresponding BH₂PH⁻ state.

Unfortunately there seem to be no experimental data for comparison with the results in Table IV. In a theoretical study of the ground state, Hinde, Pross, and Radom²⁴ obtained the following structural parameters with a **4-31** G basis set: BN, **1.360 A;** BH,, **1.241 A;** BH2, **1.228** A; NH, **1.016 A;** NBH,, **126.4';** NBH2, **121.2';** BNH, **115.1'.**

Table V summarizes the energies of the various states studied in this investigation.

Comparison of **B-N and B-P** *r* **Bond Energies**

Not too many years ago a popular textbook stated that phosphorus had no known $p\pi$ - $p\pi$ bonds, but recent studies have shown that the phosphorus atom can form planar structures with remarkably strong π bonds. This characteristic is usually masked by the much stronger tendency of phosphorus to form pyramidal structures having lone pairs. Schade and Schleyer²⁵ concluded that 'Planarized phosphino groups are **good** to excellent pr-donors,

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⁽²⁴⁾ Hinde, A. L.; **Pross,** A.; Radom, **L.** J. *Comput. Chem.* **1980,** *I,* **118.**

⁽²⁵⁾ Schade, **C.;** Schleyer, P. v. R. J. *Chem. SOC., Chem. Commun.* **1987, 1399.**

Table V. Energies of BH₂NH₂ and BH₂NH⁻ States^a

	energy				
state	SCF	CISD	Davidson cor		
$BH2NH2$, ground	-81.51055 (-81.51516)	-81.77948 (-81.79774)	-81.80228 (-81.82239)		
$BH2NH2, Cr$ rotational	-81.46417	-81.72890	-81.75072		
$BH2NH2, C2$ rotational	-81.45770	-81.72056	-81.74193		
$BH2NH-$, ground	-80.86682 (-80.87971)	-81.13983 (-81.16894)	-81.16533 (-81.19707)		
$BH2NH-$, inversion	-80.83251 (-80.84808)	-81.10329 (-81.13624)	-81.12811 (-81.16395)		

a **Results with the DZ + 2P + diff basis set are listed in parentheses: other results were obtained with the DZ** + **P basis set. Energies are in hartrees.**

sometimes comparable to amines." Coolidge and Borden²⁶ have found that in borylphosphine, $BH₂PH₂$, the conjugation energy and the pyramidalization energy are similar in magnitude (but opposite in sign) at various pyramidalization angles. In our own study of borylphosphine,² we found that the B-P π bond is about as strong as the B-N π bond, but it was difficult to compare the twobecauseof considerable uncertaintyabout the latter. (Earlier studies had a spread of about 10 kcal/mol, from 33.8^{21} to 43.1^{19} kcal/mol.)

Now that we have examined the boranamine molecule with the aid of extensive basis sets and configuration interaction computations, we find that the $B-P \pi$ bond is actually somewhat *stronger* than the B-N π bond. We here use a common measure of π -bond energy-the energy difference between planar BH₂- XH_2 and the 90° twisted (C_{2v}) BH₂XH₂. With Davidsoncorrected energies, the B-N π bond energy is 37.9 kcal/mol (Table III), compared to a B-P π bond energy of 40.5 kcal/mol.² (Similar differences are found with SCF and CISD energies.)

Of course, the question arises, are these mainly $p\pi-p\pi$ or $p\pi$ $d\pi$ bonds? Our studies indicate that they are overwhelmingly of $p\pi$ - $p\pi$ type. With the DZ basis set, which has no d orbitals, the comparable energies are 39.7 kcal/mol for B-N (this study) and 40.8 kcal/mol for B-P.²²

The fact that the SCF π -bond energies are somewhat lower than those with configuration interaction indicates that hyperconjugation may be of some minor importance in these molecules. On the other hand, the absence of any significant variation of the difference between the B-N and B-P results at different levels of theory suggests that the contribution of hyperconjugation is rather similar in the two molecules.

Another common measure of bond strength is bond length. Using the $DZ + P$ results for $BH₂NH₂$, we find that the B-N bond is 4.3% shorter in the planar form than in the twisted (C_{2v}) form. The corresponding shortening of the $B-P$ bond in $BH₂$ - PH_2 is 7.8%, again indicating that the B-P π bond is the stronger of the two.

A contrary trend would seem to be provided by examination of the vibrational frequencies. Using **DZ** + P SCF data, the BN

Table VI. Dipole Moments" and Mulliken Atomic Charges

state	dipole moment	com- ponent ^b	в	N	each H on B	each H on N
$BH2NH2$, planar	1.74	-1.74	0.06	-0.47	-0.03	0.24
rot tr. C_r	1.59	-0.16	0.20		$-0.56 -0.02$ (H ₁) -0.04 (H ₂)	0.21
rot tr, C_{2n}	0.96	-0.96	0.22	-0.64	-0.04	0.24
$BH2NH-$, planar	1.57	0.05	-0.23		-0.62 -0.14 (H ₁) -0.12 (H ₂)	0.10
inv tr	1.79	-1.79	-0.21	-0.64	-0.15	0.16

^{*a*} Dipole moments are in D. ^{*b*} Component of the dipole moment along **the BN internuclear axis, taken from N to B.**

stretching frequency increases by 23% **on** going from the twisted (C_{2v}) form to the planar form for $BH₂NH₂$ but only by 15% for $BH₂PH₂$. However, these frequencies include the effect of the larger phosphorus mass on the frequency. When the BN stretching constant from the force constant matrix is examined, the corresponding changes are 28% (from 0.370 to 0.473 atomic units) and 33% (from 0.184 to 0.245 atomic units), respectively, indicating a slightly tighter BP bond. Of course these are only measures of the shape of the potential well in the vicinity of the energy minima and not the well depth itself.

As still another measure of π -bond strength, consider what happens to the HOMO energy when we change from the planar to twisted (C_{2v}) structure. For the planar form, the HOMO is the 1b₁ (BH₂NH₂) or 2b₁ (BH₂PH₂) MO, occupied by the π bonding electrons. For the twisted form, the HOMO is the $2b_2$ $(BH₂NH₂)$ or 3b₂ $(BH₂PH₂)$ MO, occupied by electrons in a sort of bifurcated lone pair on the nitrogen or phosphorus atom, with the electron density distributed equally on either side of the XH₂ plane.

For $BH₂NH₂$ the HOMO energy changes from -11.86 eV in the planar form to -9.66 eV in the twisted form, an increase of 2.20 eV. For $BH₂PH₂$ the corresponding data are -8.93 and -7.54 eV, or an increase of 1.39 eV. Thus the π -bonding electrons in planar $BH₂NH₂$ lie at a much more negative energy, relative to the twisted form, that do the π -bonding electrons in planar $BH₂PH₂$ relative to its twisted form. Taking these data in isolation, one would conclude that the BN π bond is the stronger of the two. The fact that the total energy of the molecule indicates the opposite result, as discussed above, shows that one cannot isolate the electronic structure changes taking place to a single canonical MO energy.

Dipole Moments and Atomic Charges

In each of the structures studied here, the Mulliken populations indicate that the nitrogen atom is more negative than the boron atom. But, because of the influence of the hydrogen atoms, the polarity along the BN internuclear axis has the direction $B^- - N^+$, with one exception. That exception occurs for the planar $BH₂NH$ anion. The relevant data are summarized in Table VI.

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⁽²⁶⁾ Coolidge, M. B.; Borden, W. T. *J. Am. Chem.* **Soc. 1990,** *112,* **1704.**